

A Framework for Hardware Efficient Reusable IP Core for Grayscale Image CODEC

Anirban Sengupta, *Member IEEE*, Dipanjan Roy, *Student Member IEEE*, Saraju Mohanty, Senior *Member IEEE*, Peter Corcoran, *Fellow IEEE*

Abstract— This paper proposes two major novelties: (a) mathematical framework for hardware resource efficient IP core based image compression and decompression (CODEC). The framework includes CODEC functions that are capable to determine the pixel intensities of a compressed gray scale image using significantly lesser hardware resources. Digital pixel values of original image is fed as an input to the functions of proposed IP framework and compressed digital pixel values of compressed image is generated. Similarly, digital pixel values of compressed image are fed into another functions of proposed framework for image decompression (b) the second novelty is using the derived IP functions to propose designs of reusable IP cores for complete Haar Wavelet Transformation (HWT) based lossy image CODEC. Testing of images from various datasets (NASA, medical applications etc.) in terms of hardware resources, image quality and compression efficiency have indicated that proposed IP core framework was successful in achieving hardware efficient CODEC compared to JPEG and conventional HWT CODECs.

Index Terms— IP core, CODEC, hardware efficient, pixel intensity

I. INTRODUCTION

WITH the advancement of multi-media technologies and digital systems like digital camera, smart phone, scanner, tablets etc. high-resolution images can be captured easily [15, 19, 20]. Due to the better quality, these high-resolution images occupy large storage space, take high transmission time and large bandwidth to upload/download an image [13] [14]. An efficient Intellectual Property (IP) block/reusable core [11] [12] for image compression and decompression can compute (generate) the compressed image as well as reconstruct it through a single step computation each while preserving the compression efficiency and quality parameters of a captured image. Image compressions are of two types: a) lossless, where no data loss is occurred; b) lossy, where less relevant data are discarded. Cameras in medical imaging [6], satellite imaging, forensic imaging use lossless image compression [7] [8], while camera in smart phones, tables, digicam, scanner etc uses lossy image compression.

In the year 2000 Joint Photographic Experts Group (JPEG) proposed Discrete Wavelet Transformation (DWT) based image compression technique [1] [2] [3]. Haar Wavelet Transformation (HWT) based image compression is one of the

efficient forms of DWT [9] based image compression technique [10]. HWT decomposes each signal into two components, one is called average (approximation) or trend and the other is known as difference (detail) or fluctuation.

Wavelet based image compression for volumetric medical imaging is discussed in [4]. Both lossy and lossless image compression is performed through directional wavelet transforms, block-based intra-band prediction and arbitrary decomposition structures. A new algorithm is proposed in [5] to select a threshold value through statistical analysis. The proposed algorithm is capable to maximize the compression ratio while minimizing the redundancy. Further reduction of image details is also achieved through Huffman encoding. None of these aforementioned approaches propose any functions for dedicated HWT-based image compressing and decompressing hardware or presents the design flow of an IP core for image compression and decompression.

Rest of the paper is organized as follows: Section II highlights the novelties of proposed approach, Section III introduces proposed novel framework for IP block based HWT lossless image compression; Section IV introduces proposed novel IP core based design process for HWT-based image compressor and decompressor. Section V presents the analysis and results while Section VI presents the conclusion.

II. NOVEL CONTRIBUTIONS OF THIS PAPER

a) Proposes multiple functions for IP block based HWT image compression and image reconstruction. The IP functions are capable to directly determine the pixel intensities of a compressed gray scale image and can be used as a 'back box' in image processing tools as library where uncompressed digital pixel values of original image is fed as input to the IP block (representing a set of functions) and compressed digital pixel values of compressed image is generated. Similarly, digital pixel values of compressed image are fed into another IP black box (representing a set of functions) for image reconstruction.

b) Using the derived IP functions for both compression/decompression, to propose the system design of a dedicated reusable soft IP cores for complete HWT based image compression and image reconstruction. Both designs have been successfully tested on Intel Cyclone FPGA. The IP core designs can be used directly as a macro-block (CODEC) in SoCs or standalone ASICs. The reduction of designer effort obtained when applying proposed IP core based compression method compared to normal hardware based HWT and DCT/JPEG based compression is shown in Table I, Table II

This work is financially supported by Council of Scientific and Industrial Research under sanctioned grant no. 22/730/17/EMR-II.

A. Sengupta (asengupt@iiti.ac.in) and D. Roy are with Computer Science and Engineering at Indian Institute of Technology, Indore. SP Mohanty is with Computer Science and Engineering at University of North Texas, Denton, USA. Peter Corcoran is with Engineering & Informatics at NUI Galway.

Table1.Reduction of designer effort obtained when applying proposed IP based method in HWT Hardware Image Compression

Proposed IP core based hardware HWT based image CODEC		HWT matrix multiplication hardware based image CODEC		Proposed IP core based hardware HWT based image CODEC		HWT matrix multiplication hardware based image CODEC	
Resources required for IP core 1 based Image compression	Resources required for IP core 2 based Image decompression	Resources required for Image compression	Resources required for Image decompression	Speed of computation of IP core 1 for image compression	Speed of computation of IP core 2 for image decompression	Speed of computation for image compression	Speed of computation for image decompression
4 ASU, 4 Mul	4 ASU, 2 Adder, 2 Mul	512 Mul, 511 Adder	512 Mul, 511 Adder	4 pixels per execution	4 pixels per execution	1 pixel per execution	1 pixel per execution

Table2.Reduction of designer effort obtained when applying proposed IP based method in JPEG Hardware Image Compression

Proposed IP core based hardware HWT based image CODEC		JPEG/DCT matrix multiplication hardware based image CODEC		Proposed IP core based hardware HWT based image CODEC		JPEG/DCT matrix multiplication hardware based image CODEC	
Resources required for IP core 1 based Image compression	Resources required for IP core 2 based Image decompression	Resources required for Image compression	Resources required for Image decompression	Speed of computation of IP core 1 for image compression	Speed of computation of IP core 2 for image decompression	Speed of computation for image compression	Speed of computation for image decompression
4 ASU, 4 Mul	4 ASU, 2 Adder, 2 Mul	8 Mul, 7 Adder	8 Mul, 7 Adder	4 pixels per execution	4 pixels per execution	1 pixel per execution	1 pixel per execution

Further reduction in designer effort when applying proposed IP block based compression compared to normal software based HWT and DCT/JPEG based compression is shown in Fig. 1. The block diagram representation of proposed IP block/core based HWT image compression and decompression is shown in Fig.2.

III. PROPOSED FRAMEWORK FOR IP BASED HWT LOSSY IMAGE COMPRESSION

A. Problem Formulation

For a gray scale input image of size NxN design an IP core for HWT-based image compression and decompression.

B. Processing Input Image

In the proposed approach, an NxN gray scale digital image with 8-bit depth is considered as input. An NxN matrix is generated by calculating the pixel intensity of each coordinate of the input image. Fig. 3 shows a generic 512x512 input image in the form of a matrix (A). The subscript and superscript of each element indicate the row number and column number of the element respectively. For example, the pixel intensity of 3rd row and 510th column of matrix 'A' is represented by element $m_{3^{510}}$. In a gray image, the pixel values lay between 0 and 255, where 255 indicates pure white and 0 indicates pure black.

C. Background on Haar Wavelet Transformation

In the process of Haar wavelet based transformation of input data two types of coefficient are generated: a) scaling coefficient and b) wavelet coefficient. Scaling coefficient represents the sum of two consecutive data samples and divided by two while wavelet coefficient represents the difference of two consecutive data samples and divided by two. Thus scaling coefficients represent the high-frequency signals known as coarse details of the data and wavelet coefficients represent the low-frequency signals known as finer details of the data.

2D-Haar wavelet transformation is comprised of: forward transformation of data and inverse transformation of data. Forward transformation is a two-step process i.e. level 1

forward transformation on input data and level 2 forward transformation on level 1 transformed data. Similarly, inverse transformation is also a two-step process i.e. level 1 inverse transformation on compressed data and level 2 inverse transformation on level 1 decompressed data.

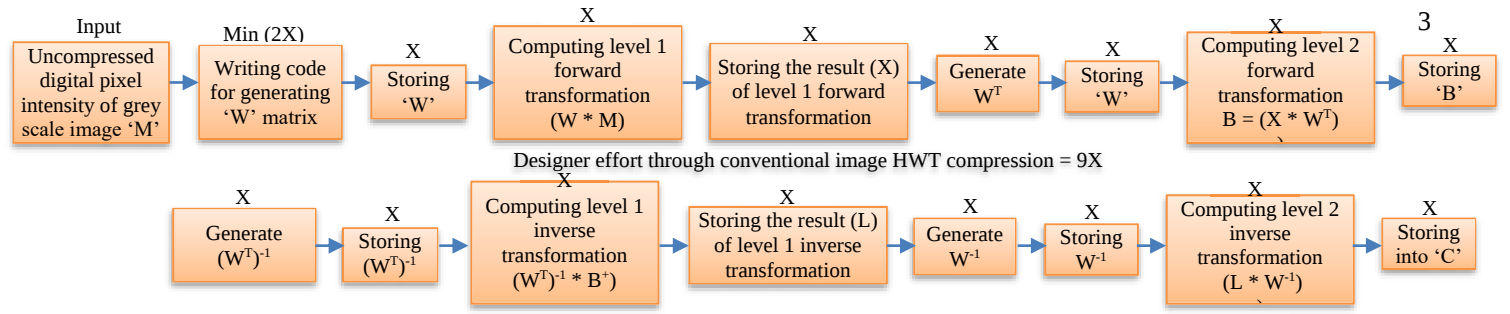
D. Proposed IP Core Design for HWT-based Image Compression

In the proposed IP core design for HWT-based image compression, we have introduced two functions to perform pixel intensity computation for level 1 forward transformation. The proposed functions transform the input image column-wise i.e. compute scaling coefficient by adding two vertically consecutive pixel intensities and divided by two for 1 to N/2th row, and compute wavelet coefficient by subtracting two vertically consecutive pixel intensities and divided by two for (N/2+1)th to Nth row. Thus divides the input image horizontally into two halves. The upper half represents the coarse details containing scaling coefficients (high frequencies) and the lower half represents the finer details containing wavelet coefficients (low frequencies). The proposed functions to perform pixel intensity computation for level 1 forward transformation are:

$$X_n^p = \left(\frac{m_{2n}^p + m_{2n-1}^p}{2} \right) \quad (1)$$

$$X_{\frac{N}{2}+i}^p = \left(\frac{m_{\frac{N}{2}+i-j+1}^p - m_{\frac{N}{2}+i-j}^p}{2} \right) \quad (2)$$

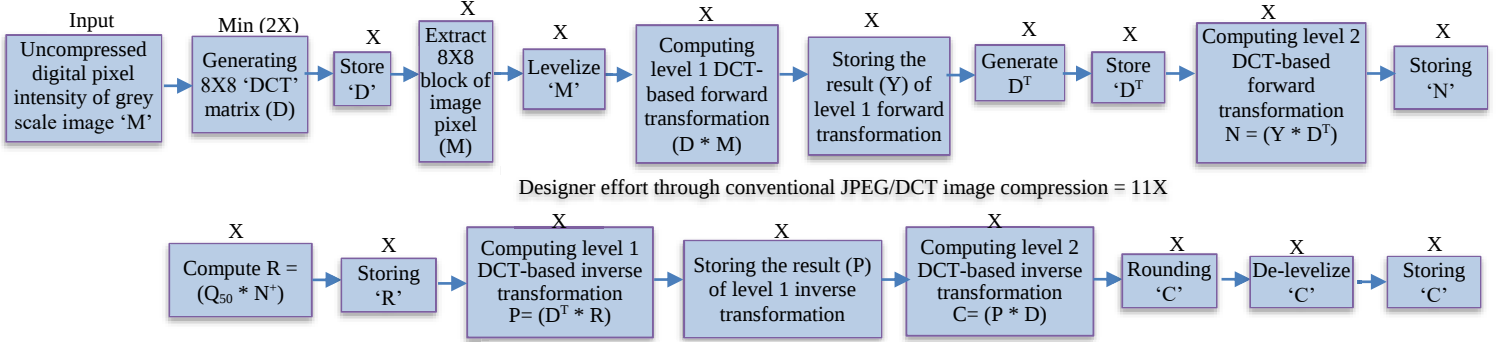
Where, N is the dimension of the square input image; n is the variable ranging from 1 to N/2, increases in every row; i is the variable ranging from 1 to N/2, increases in every row; p is the variable ranging from 1 to N, increases in every column; j is the variable ranging from N/2 to 1, decreases as 'i' increases. Eqn.1 is used for calculating 1 to N/2th row and Eqn.2 is used for calculating (N/2+1)th to Nth row of the input image. The corresponding level 1 forward transformation image in the form of matrix 'X' is shown in Fig.4 where calculation of pixel intensity is performed based on the aforementioned equations.



Note: B^+ is the image matrix after quantization and rounding

Designer effort through conventional image HWT decompression = 8X

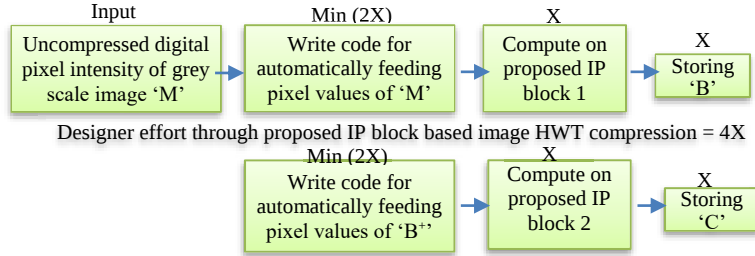
(a) Total designer effort for conventional lossy image HWT CODEC = min (17X) + 1X (Thresholding) = min (18X)



Note: N^+ is the image matrix after quantization and rounding

Designer effort through conventional JPEG/DCT image decompression = 8X

(b) Total designer effort for lossy JPEG image CODEC = min (19X) + 2X (Quantization) + 1X (Rounding) = min (22X)



Note: B^+ is the image matrix after Thresholding

Designer effort through proposed IP block based image HWT decompression = 4X

(c) Total designer effort for lossy image CODEC through proposed approach IP based HWT CODEC = min (8X) + 1X (Thresholding) = min (9X)

Fig.1. Reduction of designer effort obtained when applying proposed IP based method in Software Image Compression (Reduction of 9X and 13X compared to conventional HWT image compression and JPEG/DCT image compression respectively)

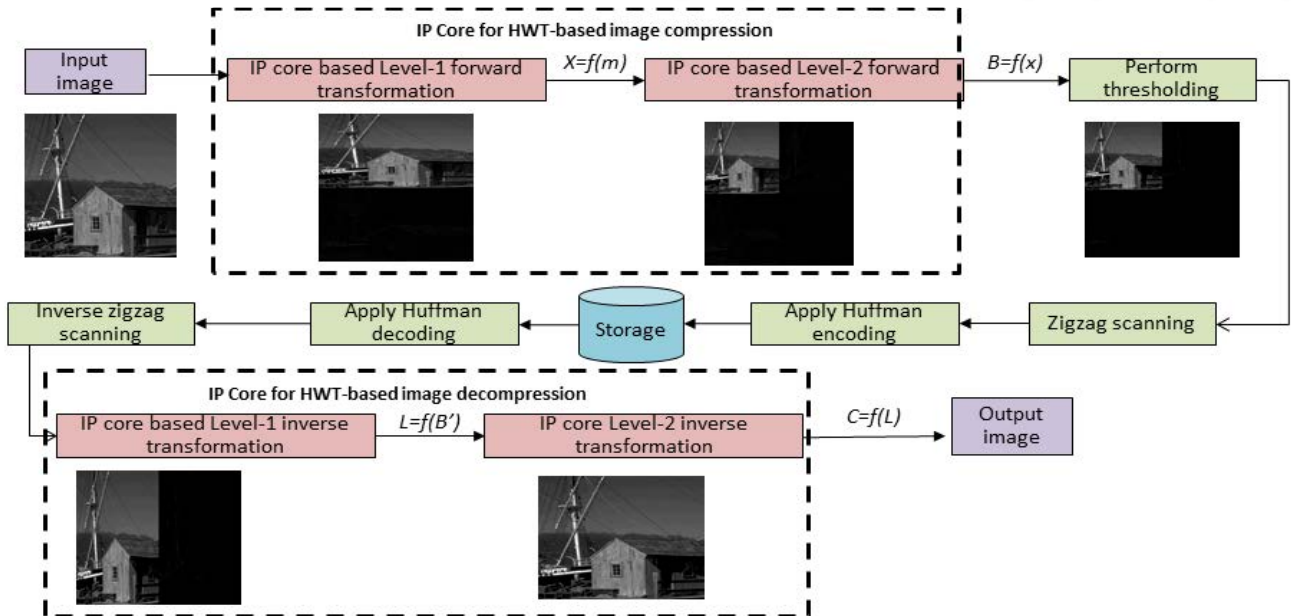


Fig. 2. Framework for IP based image compression and decompression through dedicated hardware

$$A = (512 \times 512) \begin{bmatrix} m_1^1 & m_1^2 & m_1^3 & \dots & m_1^{510} & m_1^{511} & m_1^{512} \\ m_2^1 & m_2^2 & m_2^3 & \dots & m_2^{510} & m_2^{511} & m_2^{512} \\ m_3^1 & m_3^2 & m_3^3 & \dots & m_3^{510} & m_3^{511} & m_3^{512} \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ m_{256}^1 & m_{256}^2 & m_{256}^3 & \dots & m_{256}^{510} & m_{256}^{511} & m_{256}^{512} \\ m_{257}^1 & m_{257}^2 & m_{257}^3 & \dots & m_{257}^{510} & m_{257}^{511} & m_{257}^{512} \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ m_{512}^1 & m_{512}^2 & m_{512}^3 & \dots & m_{512}^{510} & m_{512}^{511} & m_{512}^{512} \end{bmatrix}$$

Fig. 3. Generic pixel value of fa 512x512 image

intensity computation for level 2 forward transformations on the level 1 transformed image. The proposed functions transform the level 1 transformed image row-wise i.e. compute scaling coefficient by adding two horizontally consecutive pixel intensities and divided by two for 1 to $N/2^{\text{th}}$ column, and compute wavelet coefficient by subtracting two horizontally consecutive pixel intensities and divided by two for $(N/2+1)^{\text{th}}$ to N^{th} column. Thus divides each half of level 1 transformed image into vertically two halves and finally divides the input image into four quarters. The upper-left quarter contains the scaling coefficients of scaling coefficient (high-high frequencies), the upper-right quarter contains the scaling coefficients of wavelet coefficient (high-low frequencies), the lower-left quarter contains the wavelet coefficients of scaling coefficient (low-high frequencies) and the lower-right quarter contains the wavelet coefficients of wavelet coefficient (low-low frequencies). The proposed functions to perform pixel intensity computation for level 2 forward transformations are:

$$B_n^q = \left(\frac{x_n^{2q-1} + x_n^{2q}}{2} \right) \quad (3)$$

$$B_n^{\frac{N}{2}+i} = \left(\frac{x_n^{\frac{N}{2}+i-j+1} - x_n^{\frac{N}{2}+i-j}}{2} \right) \quad (4)$$

Where, N is the dimension of the square level 1 transformed image; n is the variable ranging from 1 to N, increases in

$$X = (512 \times 512) \begin{bmatrix} x_1^1 = \frac{m_1^1 + m_1^2}{2} & x_1^2 = \frac{m_1^2 + m_1^3}{2} & \dots & x_1^{512} = \frac{m_1^{512} + m_1^{512}}{2} \\ x_2^1 = \frac{m_2^1 + m_2^2}{2} & x_2^2 = \frac{m_2^2 + m_2^3}{2} & \dots & x_2^{512} = \frac{m_2^{512} + m_2^{512}}{2} \\ \dots & \dots & \dots & \dots \\ x_{256}^1 = \frac{m_{256}^1 + m_{256}^2}{2} & x_{256}^2 = \frac{m_{256}^2 + m_{256}^3}{2} & \dots & x_{256}^{512} = \frac{m_{256}^{512} + m_{256}^{512}}{2} \\ x_{257}^1 = \frac{m_{257}^1 - m_{257}^2}{2} & x_{257}^2 = \frac{m_{257}^2 - m_{257}^3}{2} & \dots & x_{257}^{512} = \frac{m_{257}^{512} - m_{257}^{512}}{2} \\ \dots & \dots & \dots & \dots \\ x_{512}^1 = \frac{m_{512}^1 - m_{512}^2}{2} & x_{512}^2 = \frac{m_{512}^2 - m_{512}^3}{2} & \dots & x_{512}^{512} = \frac{m_{512}^{512} - m_{512}^{512}}{2} \end{bmatrix}$$

Fig. 4. Forward HWT-based level 1 transformed image matrix

$$B = (512 \times 512) \begin{bmatrix} b_1^1 = \frac{x_1^1 + x_1^2}{2} & \dots & b_1^{256} = \frac{x_1^{511} + x_1^{512}}{2} & b_1^{257} = \frac{x_1^2 - x_1^1}{2} & \dots & b_1^{512} = \frac{x_1^{512} - x_1^{511}}{2} \\ b_2^1 = \frac{x_2^1 + x_2^2}{2} & \dots & b_2^{256} = \frac{x_2^{511} + x_2^{512}}{2} & b_2^{257} = \frac{x_2^2 - x_2^1}{2} & \dots & b_2^{512} = \frac{x_2^{512} - x_2^{511}}{2} \\ \dots & \dots & \dots & \dots & \dots & \dots \\ b_{256}^1 = \frac{x_{256}^1 + x_{256}^2}{2} & \dots & b_{256}^{256} = \frac{x_{256}^{511} + x_{256}^{512}}{2} & b_{256}^{257} = \frac{x_{256}^2 - x_{256}^1}{2} & \dots & b_{256}^{512} = \frac{x_{256}^{512} - x_{256}^{511}}{2} \\ b_{257}^1 = \frac{x_{257}^1 + x_{257}^2}{2} & \dots & b_{257}^{256} = \frac{x_{257}^{511} + x_{257}^{512}}{2} & b_{257}^{257} = \frac{x_{257}^2 - x_{257}^1}{2} & \dots & b_{257}^{512} = \frac{x_{257}^{512} - x_{257}^{511}}{2} \\ \dots & \dots & \dots & \dots & \dots & \dots \\ b_{512}^1 = \frac{x_{512}^1 + x_{512}^2}{2} & \dots & b_{512}^{256} = \frac{x_{512}^{511} + x_{512}^{512}}{2} & b_{512}^{257} = \frac{x_{512}^2 - x_{512}^1}{2} & \dots & b_{512}^{512} = \frac{x_{512}^{512} - x_{512}^{511}}{2} \end{bmatrix}$$

Fig. 5. Forward HWT-based level 2 transformed image matrix

every row; i is the variable ranging from 1 to $N/2$, increases in every column; q is the variable ranging from 1 to $N/2$, increases in every column; j is the variable ranging from $N/2$ to 1, decreases as 'i' increases. Eqn.3 is used for calculating 1 to $N/2^{\text{th}}$ column and Eqn.4 is used for calculating $(N/2+1)^{\text{th}}$ to N^{th} column of the level 1 transformed image. The corresponding level 2 forward transformation image in the form of matrix 'B' is shown in Fig.5 where calculation of pixel intensity is performed based on the aforementioned equations. The HWT-based compressed image matrix (B) can be generated in one step computation from the input image matrix (A) through the following proposed functions:

$$B = \left(\left(\frac{m_{2n}^q + m_{2n-1}^q}{2} \right) + \left(\frac{m_{2n}^p + m_{2n-1}^p}{2} \right) / 2 \right) \quad (5)$$

$$B = \left(\left(\frac{m_{2n}^q + m_{2n-1}^q}{2} \right) - \left(\frac{m_{2n}^p + m_{2n-1}^p}{2} \right) / 2 \right) \quad (6)$$

$$B = \left(\left(\frac{m_{\frac{N}{2}+i-j+1}^q - m_{\frac{N}{2}+i-j}^q}{2} \right) + \left(\frac{m_{\frac{N}{2}+i-j+1}^p - m_{\frac{N}{2}+i-j}^p}{2} \right) / 2 \right) \quad (7)$$

$$B = \left(\left(\frac{m_{\frac{N}{2}+i-j+1}^q - m_{\frac{N}{2}+i-j}^q}{2} \right) - \left(\frac{m_{\frac{N}{2}+i-j+1}^p - m_{\frac{N}{2}+i-j}^p}{2} \right) / 2 \right) \quad (8)$$

Where, N is the dimension of the square input image matrix; n is the variable ranging from 1 to $N/2$, increases in every row; i is the variable ranging from 1 to $N/2$, increases in every row; p is the odd variable ranging from 1 to N, increases in every column; q is the even variable ranging from 2 to N, increases in every column; j is the variable ranging from $N/2$ to 1, decreases as 'i' increases.

To generate the compressed image matrix 'B', **Eqn. 5** is used for calculating intensity of pixels corresponding to both row and column index 1 to $N/2$; **Eqn. 6** is used for calculating intensity of pixels corresponding to row index 1 to $N/2$ and column index $>$ than $N/2$ to N; **Eqn. 7** is used for calculating intensity of pixels corresponding to row index $>$ than $N/2$ to N and column index 1 to $N/2$; **Eqn. 8** is used for calculating intensity of pixels corresponding to both row and column index $>$ than $N/2$ to N. Those aforementioned functions can be used as a dedicated macro block in any image processing toolbox software like Matlab, OpenCV directly to perform HWT-based image compression.

E. Compression and Decompression of Image Data

Thresholding is performed on the compressed image pixel (matrix) 'B' using function 'f', where 'f' is defined as follows:

$$B' = f(B, T) = \begin{cases} B, & b_n^p > T \\ 0, & b_n^p \leq T \end{cases} \quad (9)$$

Where, B' are the compressed image pixels after applying threshold based on the aforementioned function and 'T' is the hard threshold value. The compressed image matrix B' is then converted from a 2D matrix to a 1D array through zigzag scanning. Thereafter the 1D array is encoded through Huffman encoding in order to generate the bit stream data of the compressed image to store it in a storage device. To decompress the image from the stored data, the stored bit stream data is decoded through Huffman decoding and then the compressed image matrix B' is reconstructed through inverse zigzag scanning.

F. Proposed IP Core Design for HWT-based Image Decompression (Image reconstruction)

HWT-based image decompression can be achieved in two different ways. One way is, combining upper-left with lower left quarter together as well as upper-right with lower-right quarter together. This divides the level 1 decompressed image vertically into two halves (left half and right half), subsequently then combining left half and right half together thus generating the final decompressed image. Second way is, combining upper-left with upper-right quarter together and lower-left with lower-right quarter together. This divides the level 1 decompressed image horizontally into two halves (upper half and lower half), subsequently then combining upper half and lower half together thus generating the final decompressed image. In the proposed IP core design for HWT-based image decompression, we have introduced two functions for each of the cases to perform pixel computation for level 1 inverse transformation and two functions for each of the cases to perform pixel computation for level 2 inverse transformations. For the first case, the proposed functions for level 1 inverse transformation transforms the compressed image column-wise i.e. subtract i^{th} and $(N/2+i)^{\text{th}}$ row's pixel intensity for odd rows, and add i^{th} and $(N/2+i)^{\text{th}}$ row's pixel intensity for even rows. Thus level 1 HWT-based inverse transformation represents the level 1 decompressed image into two halves. The left half represents the coarse details containing scaling coefficients (high frequencies) and the right

half represents the finer details containing wavelet coefficients (low frequencies). The proposed functions for level 2 inverse transformation transforms the level 1 transformed image row-wise i.e. subtract i^{th} and $(N/2+i)^{\text{th}}$ column's pixel intensity for odd columns, and add i^{th} and $(N/2+i)^{\text{th}}$ column's pixel intensity for even columns. Thus level 2 HWT-based inverse transformations construct the complete decompressed image.

For the next case, the proposed functions for level 1 inverse transformation transforms the compressed image row-wise i.e. subtract i^{th} and $(N/2+i)^{\text{th}}$ column's pixel intensity for odd columns, and add i^{th} and $(N/2+i)^{\text{th}}$ column's pixel intensity for even columns. Thus level 1 HWT-based inverse transformation represents the decompressed image into two halves. The upper half represents the coarse details containing scaling coefficients (high frequencies) and the lower half represents the finer details containing wavelet coefficients (low frequencies). The proposed functions for level 2 inverse transformation transforms the level 1 transformed image column-wise i.e. subtract i^{th} and $(N/2+i)^{\text{th}}$ row's pixel intensity for odd rows, and add i^{th} and $(N/2+i)^{\text{th}}$ row's pixel intensity for even rows. Thus level 2 HWT-based inverse transformations construct the complete decompressed image. The proposed functions to perform first type of pixel intensity computation for level 1 inverse transformation are:

$$L = \left(b'_x{}^z - b'_{\frac{N}{2}+x}{}^z \right) \quad (10)$$

$$L = \left(b'_x{}^z + b'_{\frac{N}{2}+x}{}^z \right) \quad (11)$$

Where, N is the dimension of the square compressed image matrix; z is the variable ranging from 1 to N, increases in every column; x is the variable ranging from 1 to N/2, increases in every alternate row. Eqn.10 is used for calculating the pixel value of odd rows and Eqn.11 is used for calculating the pixel value of even rows of the compressed image. The corresponding level 1 decompressed image in the form of matrix 'L' is shown in Fig.6 where calculation of each pixel is performed based on the aforementioned equations. The proposed functions to perform first type of pixel intensity computation for level 2 inverse transformations are:

$$C = \left(l_x^z - l_x^{\frac{N}{2}+z} \right) \quad (12)$$

$$C = \left(l_x^z + l_x^{\frac{N}{2}+z} \right) \quad (13)$$

Where, N is the dimension of the square level 1 decompressed image matrix; z is the variable ranging from 1 to N/2, increases in every alternate column; x is the variable ranging from 1 to N, increases in every row. Eqn.12 is used for calculating the pixel value of odd columns and Eqn.13 is used for calculating the pixel value of even columns of the level 1 decompressed image. The corresponding level 2 decompressed image in the form of matrix 'C' is shown in Fig.7 where calculation of each pixel is performed based on the aforementioned equations. The proposed functions to perform next type of pixel intensity computation for level 1 inverse transformation are:

$$L = \left(b'_x{}^z - b'_{\frac{N}{2}+x}{}^z \right) \quad (14)$$

$$L = \begin{pmatrix} l_1^1 = (b_1^1 - b_{257}^1) & l_1^2 = (b_1^2 - b_{257}^2) & \dots & l_1^{512} = (b_1^{512} - b_{257}^{512}) \\ l_2^1 = (b_1^1 + b_{257}^1) & l_2^2 = (b_1^2 + b_{257}^2) & \dots & l_2^{512} = (b_1^{512} + b_{257}^{512}) \\ \dots & \dots & \dots & \dots \\ l_{256}^1 = (b_{128}^1 + b_{384}^1) & l_{256}^2 = (b_{128}^2 + b_{384}^2) & \dots & l_{256}^{512} = (b_{128}^{512} + b_{384}^{512}) \\ l_{257}^1 = (b_{129}^1 - b_{385}^1) & l_{257}^2 = (b_{129}^2 - b_{385}^2) & \dots & l_{257}^{512} = (b_{129}^{512} - b_{385}^{512}) \\ \dots & \dots & \dots & \dots \\ l_{511}^1 = (b_{256}^1 - b_{512}^1) & l_{511}^2 = (b_{256}^2 - b_{512}^2) & \dots & l_{511}^{512} = (b_{256}^{512} - b_{512}^{512}) \\ l_{512}^1 = (b_{256}^1 + b_{512}^1) & l_{512}^2 = (b_{256}^2 + b_{512}^2) & \dots & l_{512}^{512} = (b_{256}^{512} + b_{512}^{512}) \end{pmatrix} \quad (512 \times 512)$$

Fig. 6. Inverse HWT-based level 1 transformed image matrix

$$L = \left(b'_x{}^z + b'_x{}^{\frac{N}{2}+z} \right) \quad (15)$$

Where, N is the dimension of the square compressed image matrix; z is the variable ranging from 1 to N, increases in every column; x is the variable ranging from 1 to N/2, increases in every alternate row. Eqn.14 is used for calculating the pixel value of odd rows and Eqn.15 is used for calculating the pixel value of even rows of the compressed image. The corresponding level 1 decompressed image in the form of matrix 'L' is shown in Fig.6 where calculation of each pixel is performed based on the aforementioned equations.

The proposed functions to perform next type of pixel intensity computation for level 2 inverse transformations are:

$$C = \left(l_x^z - l_{\frac{N}{2}+x}^z \right) \quad (16)$$

$$C = \left(l_x^z + l_{\frac{N}{2}+x}^z \right) \quad (17)$$

Where, N is the dimension of the square level 1 decompressed image matrix; z is the variable ranging from 1 to N, increases in every column; x is the variable ranging from 1 to N/2, increases in every alternate row. Eqn.16 and Eqn. 17 are used for calculating the pixel value of odd rows and even rows of the level 1 decompressed image.

The HWT final decompressed image pixel intensities (of matrix C) can be generated in one step computation from compressed image matrix (B') through following proposed functions:

$$C = \left(b'_i{}^g - b'_i{}^{\frac{N}{2}+g} \right) - \left(b'_i{}^{\frac{N}{2}+g} - b'_i{}^{\frac{N}{2}+g} \right) \quad (18)$$

$$C = \left(b'_i{}^g - b'_i{}^{\frac{N}{2}+g} \right) + \left(b'_i{}^{\frac{N}{2}+g} - b'_i{}^{\frac{N}{2}+g} \right) \quad (19)$$

$$C = \left(b'_i{}^g + b'_i{}^{\frac{N}{2}+g} \right) - \left(b'_i{}^{\frac{N}{2}+g} + b'_i{}^{\frac{N}{2}+g} \right) \quad (20)$$

$$C = \left(b'_i{}^g + b'_i{}^{\frac{N}{2}+g} \right) + \left(b'_i{}^{\frac{N}{2}+g} + b'_i{}^{\frac{N}{2}+g} \right) \quad (21)$$

Where, N is the dimension of the square input image matrix; g is the variable ranging from 1 to N/2, increases in every alternate column; i is the variable ranging from 1 to N/2, increases in every alternate row. To reconstruct the each pixel value of matrix 'C' Eqn.18 is used for odd row and odd column elements, Eqn.19 is used for odd row and even column elements, Eqn.20 is used for even row and odd column elements, Eqn.21 is used for even row and even column elements of matrix B'.

IV. DESIGN OF IP CORE FOR HWT-BASED IMAGE COMPRESSOR AND DECOMPRESSOR

A. IP Core Design for HWT-based Image Compression

To design an IP core for HWT-based image compression a Data Flow Graph (DFG) for HWT-based image compression is designed based on the Eqn. 5 – Eqn.8 shown in Fig. 8 (a). The DFG is then scheduled based on designer specified

resources e.g. four 32-bit adder-subtractor unit (ASU) and four 32-bit multipliers, shown in Fig. 8(b) (Note: four 32-bit ASU and four 32-bit Mul are chosen as device support for I/O pins beyond this are not available with Cyclone II FPGA. Further, 32-bit resources have been selected because each resource operates on floating point value during computation which requires 32 bit IEEE single precision format in normalized scientific notation). The green nodes represent ASU and the blue nodes represent multiplier in the graph. The multiplexing scheme is performed on the scheduled DFG based on the resource constraints. Multiplexing scheme is the process of representing each resource with corresponding inputs and outputs. For example in Fig 8(b), operation 1 and operation 5 are computed through same functional unit i.e. ASU1. Similarly, opn 2 & opn 6; opn 3 & opn 7; opn 4 & opn 8 are computed through ASU2, ASU3, and ASU4 respectively. The datapath processor of the complete IP core is designed based on the multiplexing scheme of each system resource. Multiplexer and demultiplexer can be integrated easily into the datapath based on the multiplexing scheme. The control unit controls different components of the datapath and makes

$$C = \begin{pmatrix} c_1^1 = (l_1^1 - l_1^{257}) & c_1^2 = (l_1^1 + l_1^{257}) & \dots & c_1^{511} = (l_1^{256} - l_1^{512}) & c_1^{512} = (l_1^{256} + l_1^{512}) \\ c_2^1 = (l_2^1 - l_2^{257}) & c_2^2 = (l_2^1 + l_2^{257}) & \dots & c_2^{511} = (l_2^{256} - l_2^{512}) & c_2^{512} = (l_2^{256} + l_2^{512}) \\ \dots & \dots & \dots & \dots & \dots \\ c_{256}^1 = (l_{256}^1 - l_{256}^{257}) & \dots & \dots & c_{256}^{511} = (l_{256}^{256} - l_{256}^{512}) & c_{256}^{512} = (l_{256}^{256} + l_{256}^{512}) \\ c_{257}^1 = (l_{257}^1 - l_{257}^{257}) & \dots & \dots & c_{257}^{511} = (l_{257}^{256} - l_{257}^{512}) & c_{257}^{512} = (l_{257}^{256} + l_{257}^{512}) \\ \dots & \dots & \dots & \dots & \dots \\ c_{511}^1 = (l_{511}^1 - l_{511}^{257}) & \dots & \dots & c_{511}^{511} = (l_{511}^{256} - l_{511}^{512}) & c_{511}^{512} = (l_{511}^{256} + l_{511}^{512}) \\ c_{512}^1 = (l_{512}^1 - l_{512}^{257}) & \dots & \dots & c_{512}^{511} = (l_{512}^{256} - l_{512}^{512}) & c_{512}^{512} = (l_{512}^{256} + l_{512}^{512}) \end{pmatrix} \quad (512 \times 512)$$

Fig. 7. Inverse HWT-based level 2 transformed image matrix

synchronization between them. It is responsible for activating and deactivating signals like selector, deselector, latch strobe, enabler etc. in the datapath processor so that the components like multiplexer, demultiplexer, latch, functional unit (adder, multiplier etc.), register etc. response at the right time. Our proposed IP core design for HWT-based image compression system is shown in Fig.9 where the left block is the controller and the right block represents the datapath processor of the complete IP core design of HWT-based image compressor system. Each component of datapath processor and the control unit of HWT-based image compressor are designed using

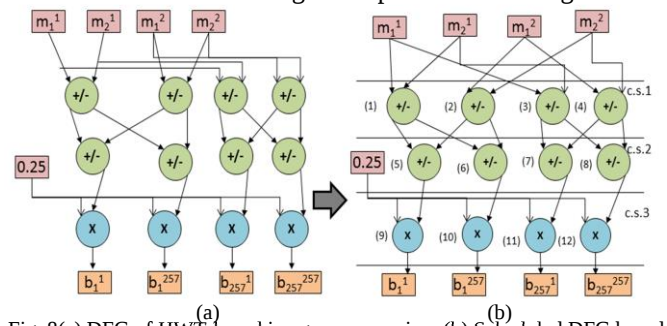


Fig. 8(a) DFG of HWT-based image compression, (b) Scheduled DFG based on 4 adder-subtractor unit and 4 multiplier

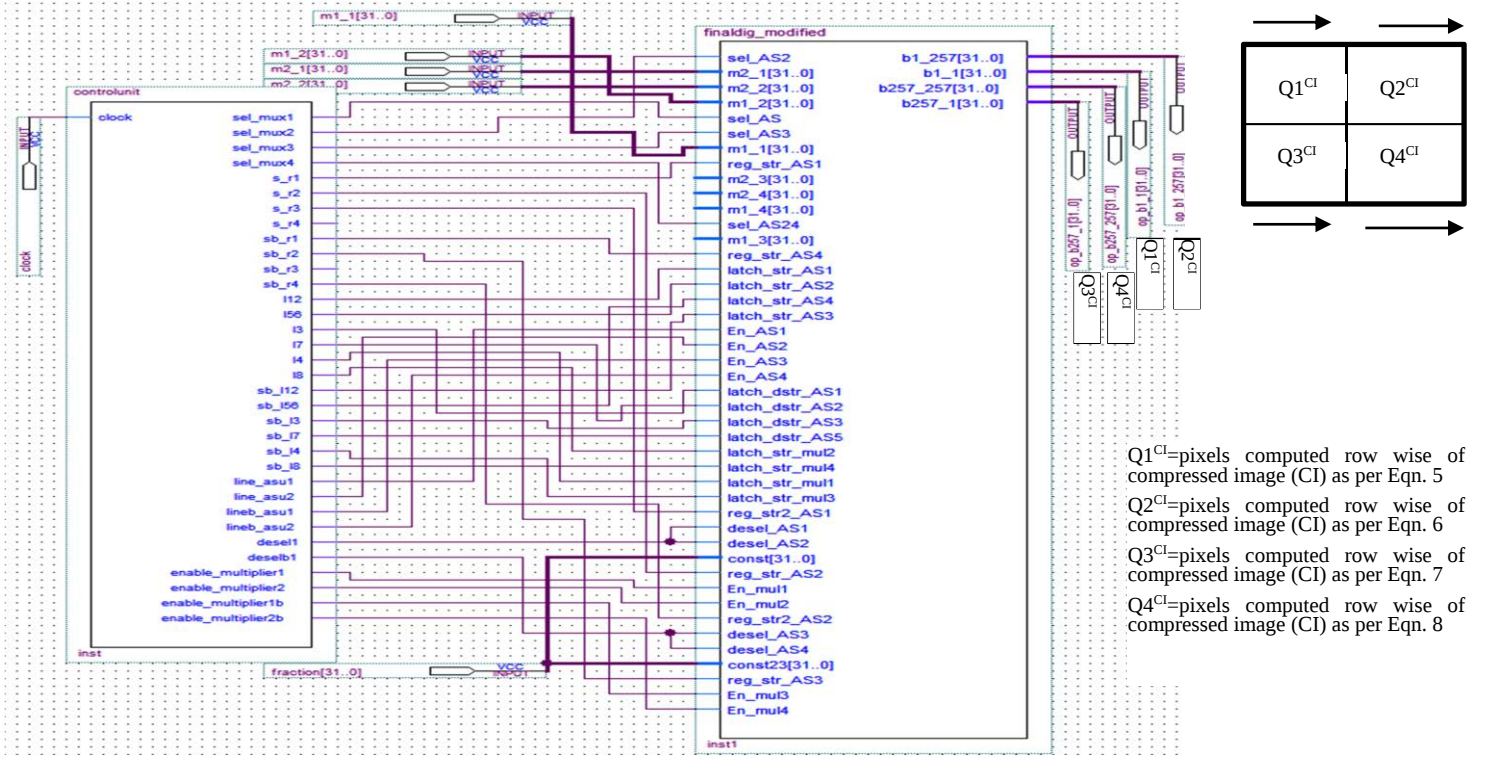


Fig.9. IP core for HWT-based image compressor system

The four output of the IP core are computed for four quarters and increases row-wise in each quarter of compressed image (CI)

VHDL as the hardware description language. The IP core is capable to accept the 8-bit digital pixel value (Note: we have considered 8-bit as it provides the maximum grayscale shades) of a grayscale input image, perform level 1 and level 2 forward transformations and generate the digital pixel value of

the corresponding compressed image. For example, as shown in Fig. 8, $m_1^1, m_2^1, m_1^2, m_2^2$ is taken as inputs which represents the pixel intensities of input image as shown in Fig. 3 and generates the outputs as $b_1^1, b_1^{257}, b_{257}^1, b_{257}^{257}$ which represents the pixel intensities of compressed image as shown

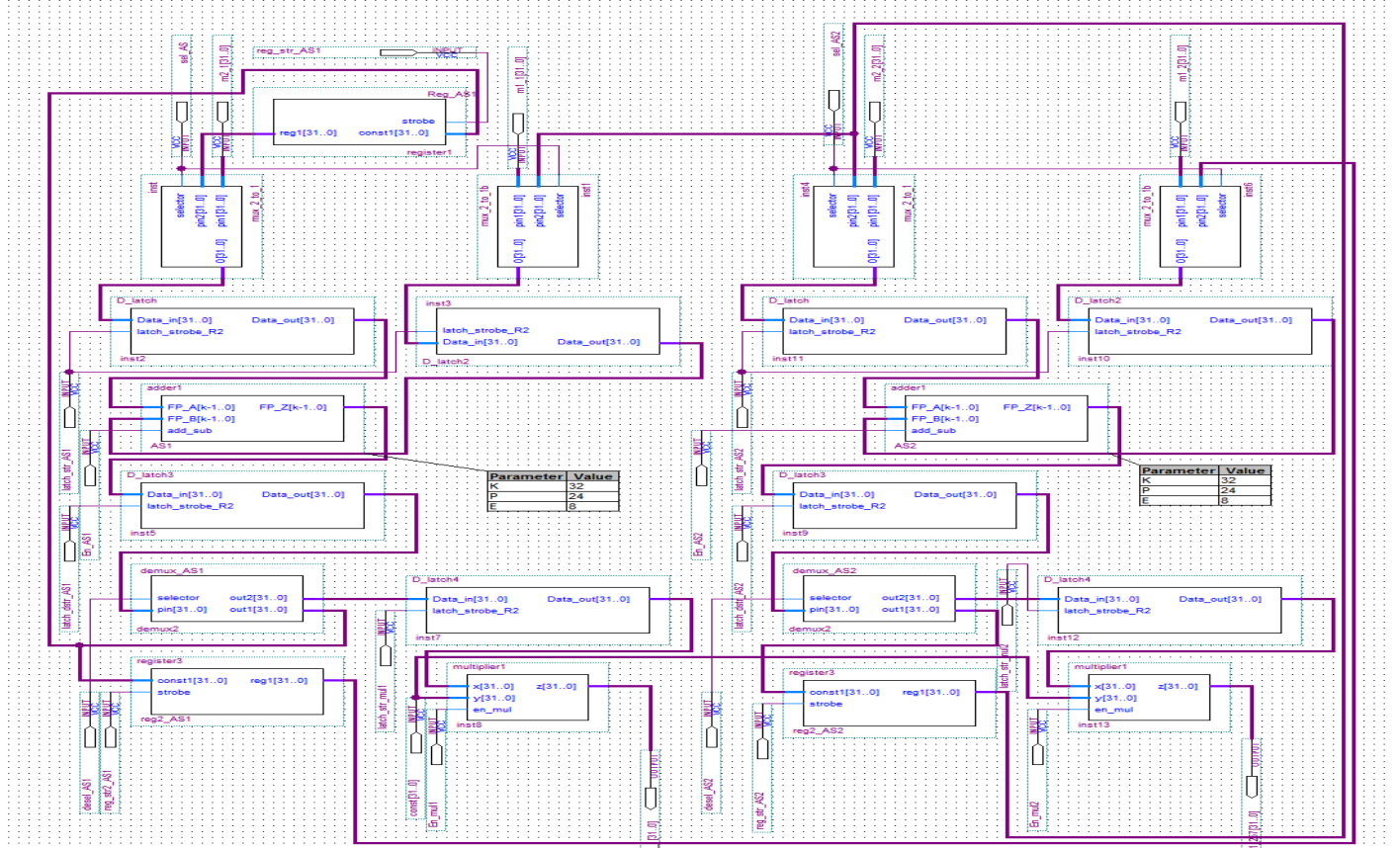


Fig10. Schematic system of datapath processor of HWT-based image compressor (computing two pixels in parallel)

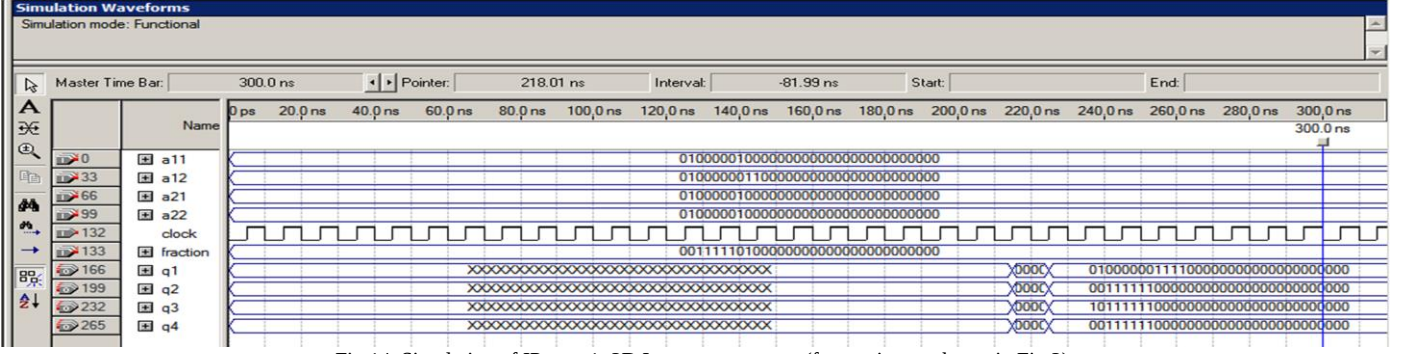


Fig.14. Simulation of IP core 1: 2D Image compressor (for test image shown in Fig.2).

Note: $q1 = b_1^1$, $q2 = b_1^{257}$, $q3 = b_{257}^1$, $q4 = b_{257}^{257}$ of compressed image

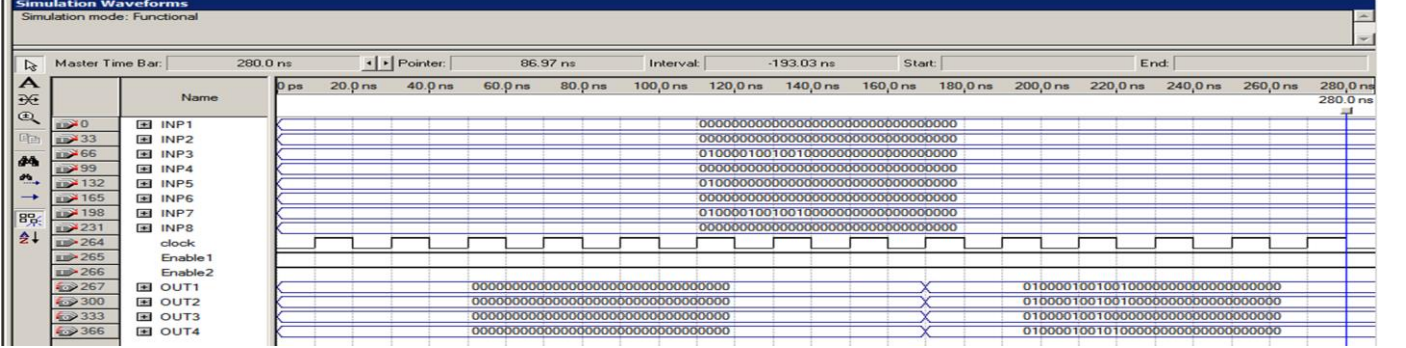


Fig.15. Simulation of IP core 2: 2D Image decompressor (for test image shown in Fig.2).

Note: $OUT1 = c_1^1$, $OUT1 = c_1^2$, $OUT1 = c_1^3$, $OUT1 = c_1^4$ of decompressed image

TABLE III
COMPARISON OF DEVICE UTILIZATION FOR PROPOSED IP CORES,
NORMAL HWT AND JPEG CODEC

IP Core	Total logic elements	Total register	Total pins
Proposed Forward HWT	4360	583	433
Proposed Inverse HWT	5329	391	384
Normal Forward HWT	33216	34593	-
Normal Inverse HWT	33216	34593	-
Standard JPEG CODEC	12121	1826	322

TABLE IV
FOR IP BASED HWT COMPRESSED IMAGE FOR T=25

Images	Original size (bits)	Compressed size (bits)	Compression efficiency (%)	MSE	PSNR
Image 1	2097152	653383	68.84	86.2	28.78
Image 2	2097152	540771	74.21	174	25.72
Image 3	3276800	812689	75.20	102	28.03
Image 4	3276800	1001555	69.44	148	26.44
Image 5	3276800	989390	69.81	61.4	30.25
Image 6	2097152	459841	78.07	239	24.34

TABLE V
FOR JPEG/DCT COMPRESSED IMAGE

Images	Original size (bits)	Compressed size (bits)	Compression efficiency (%)	MSE	PSNR
Image 1	2097152	710608	66.12	35.81	32.59
Image 2	2097152	743664	64.54	38.93	32.77
Image 3	3276800	1133296	65.41	49.9	31.15
Image 4	3276800	1733456	47.1	77.3	29.25
Image 5	3276800	1304352	60.19	35.41	32.64
Image 6	2097152	942320	55.07	96.17	28.3

compression efficiency for different threshold (T) values. Additionally, the Mean Square Error (MSE) [1,2] and the Peak Signal to Noise Ratio (PSNR) [1,2] of the compressed images is also reported. Table IV reports the comparison between the original image and the proposed IP based compressed image for hard threshold T=25 in terms of storage size in bits. Further, it also reports the compression efficiency

percentage, MSE and PSNR of all the test images. Table V reports the same quality parameters of the standard JPEG/DCT based compressed image. It can be observed that the compressed image generated through proposed HWT-based IP core achieves higher compression efficiency compared to standard JPEG/DCT method.

VI. CONCLUSION AND FUTURE WORK

In this paper, a novel IP design based HWT image compression and decompression including its mathematical framework is proposed. The models can be used as a dedicated macro block in the library of an image processing toolbox to perform end to end HWT-based image compression. Further, the designed hardware can be used as an IP core in digital camera systems to perform image compression and decompression. Our future works aims to develop IP based video CODEC through mathematical functions, followed by subsequent validation in commercial synthesis tool.

REFERENCES

- [1] S. Benchikh and M. Corinthios, "A hybrid image compression technique based on DWT and DCT transforms," *International Conference on Advanced Infocom Technology 2011*, China, 2011, pp. 1-8.
- [2] A. M. G. Hnesh and H. Demirel, "DWT-DCT-SVD based hybrid lossy image compression technique," *International Image Processing, Applications and Systems (IPAS)*, Hammamet, 2016, pp. 1-5.
- [3] ISO/IEC 15444-1 | ITU-T Rec. T.800, Information Technology - JPEG 2000 Image Coding System: Core Coding System, 2002.
- [4] T. Bruylants, A. Munteanu, and P. Schelkens, "Wavelet based volumetric medical image compression," *Signal Processing: Image Communication*, vol 31, 2015, Pages 112-133.
- [5] A. A. Nashat and N. M. H. Hassan, "Image compression based upon Wavelet Transform and a statistical threshold," *International Conference on Optoelectronics and Image Processing*, Warsaw, 2016, pp. 20-24.
- [6] A. Bilgin and M. W. Marcellin, "Applications of reversible integer wavelet transforms to lossless compression of medical image volumes," *Proceedings. 1998 IEEE International Symposium on Information Theory (Cat. No.98CH36252)*, Cambridge, MA, 1998, pp. 411.

- [7] S. Li, H. Yin, X. Fang and H. Lu, "Lossless image compression algorithm and hardware architecture for bandwidth reduction of external memory," in *IET Image Processing*, vol. 11, no. 6, 6 2017, pp. 379-388.
- [8] G. Scarmana and K. McDougall, "Exploring the application of some common raster scanning paths on lossless compression of elevation images," *2015 IEEE International Geoscience and Remote Sensing Symposium (IGARSS)*, Milan, 2015, pp. 4514-4517.
- [9] R. K. Lama, S. Shin, M. Kang, G. R. Kwon and M. R. Choi, "Interpolation using wavelet transform and discrete cosine transform for high resolution display," *2016 IEEE International Conference on Consumer Electronics (ICCE)*, Las Vegas, NV, 2016, pp. 184-186.
- [10] C. Yu and S.J. Chen, "Design of an efficient VLSI architecture for 2-D discrete wavelet transforms," in *IEEE Transactions on Consumer Electronics*, vol. 45, no. 1, pp. 135-140, Feb 1999.
- [11] A. Sengupta, "Evolution of the IP Design Process in the Semiconductor/EDA Industry [Hardware Matters]," in *IEEE Consumer Electronics Magazine*, vol. 5, no. 2, pp. 123-126, April 2016.
- [12] A. Sengupta, "Cognizance on Intellectual Property: A High-Level Perspective," in *IEEE Consumer Electronics Magazine*, vol. 5, no. 3, pp. 126-128, July 2016.
- [13] P. M. Corcoran, P. Bigioi and E. Steinberg, "Wireless transfer of images from a digital camera to the Internet via a standard GSM mobile phone," *ICCE. International Conference on Consumer Electronics (IEEE Cat. No.01CH37182)*, Los Angeles, CA, 2001, pp. 274-275.
- [14] P. M. Corcoran, P. Bigioi and E. Steinberg, "Wireless transfer of images from a digital camera to the Internet via a standard GSM mobile phone," in *IEEE Transactions on Consumer Electronics*, vol. 47, no. 3, pp. 542-547, Aug 2001.
- [15] I. Andorko, P. Corcoran and P. Bigioi, "A dual image processing pipeline camera with CE applications," *IEEE International Conference on Consumer Electronics (ICCE)*, Las Vegas, 2011, pp. 737-738.
- [16] Public Lung Database to Address Drug Response, Available. <http://www.via.cornell.edu/databases/crpf.html>.
- [17] NASA Image and Video Library, [Online]. Available. <https://images.nasa.gov/#/>
- [18] Dataset of Standard 512x512 Grayscale Test Images [Online]. Available. <http://decsai.ugr.es/cvg/CG/base.htm>, Last Accessed on 18 Aug 2017.
- [19] E. Kougianos, S. P. Mohanty, G. Coelho, U. Albalawi, and P. Sundaravadivel, "Design of a High-Performance System for Secure Image Communication in the Internet of Things (Invited Paper)", *IEEE Access Journal*, Volume 4, 2016, pp. 1222--1242.
- [20] S. P. Mohanty, "A Secure Digital Camera Architecture for Integrated Real-Time Digital Rights Management", *Elsevier Journal of Systems Architecture*, Volume 55, Issues 10-12, December 2009, pp. 468-480.

author on 300 technical publications and co-inventor on 300 granted US patents.



Magazine. He is also awarded "Outstanding Associate Editor" Award from IEEE TCVLSI, IEEE Computer Society.

Anirban Sengupta is Assistant Professor (Associate Professor appointment approved) in Computer Science and Engineering at Indian Institute of Technology Indore. He is an IEEE Distinguished Lecturer of IEEE Consumer Electronics Society and has around 130 Publications. He is currently serving as Associate Editor of IEEE Transactions on Aerospace and Electronic Systems, IEEE Access, Executive/Senior Editor of IEEE Consumer Electronics



Dipanjan Roy (S'16) is a research scholar in Computer Science and Engineering at Indian Institute of Technology (I.I.T) Indore. He worked as a software development engineer in "Amazon Development Center, Bangalore.



currently the Editor-in-Chief of IEEE Consumer Electronics Magazine.

Saraju P. Mohanty (S'00-M'04-SM'08) is a Professor at the Department of Computer Science and Engineering, University of North Texas, where he directs the NanoSystem Design Laboratory. He is author of 220 publications. He currently serves on the editorial board of IEEE Transactions on Computer-Aided Design of Integrated Circuits and Systems (TCAD) and many others. He is



Peter Corcoran is a Fellow of IEEE, the Founding Editor of IEEE Consumer Electronics Magazine and holds a Personal Chair in Electronic Engineering at the College of Engineering & Informatics at NUI Galway. He is co-